

Laplace's Equation in two variables
Cylindrical coordinates

1. An infinitely long metal cylinder of radius R is split lengthwise into two semi-cylindrical pieces. The two halves are then reassembled to form a cylinder with small gaps running parallel to the z -axis, and through the points $x=\pm R, y=0$. The upper half ($y>0$) is held at a potential of $+V_0$, and the lower half at a potential $-V_0$. Find the potential at all points $r<R$.
2. An infinitely long cylinder of radius R has its axis aligned with the z axis, and is made from a material which has a dielectric constant ϵ_r . It is placed in a uniform electric field $\mathbf{E} = E_0\mathbf{i}$. Find the electric potential and electric field everywhere.

Laplace's Equation in two variables
Spherical coordinates

3. Review the problem we did in class of a metal sphere placed in a uniform electric field. Assume now that the sphere carries a net charge $+Q$ before it is placed in the electric field.
 - a. What change(s) do you need to make to the boundary conditions?
 - b. What is the electrostatic potential outside of the sphere in this problem?